

**DETECTION OF REFLECTOR
SURFACE FROM NEAR FIELD PHASE
MEASUREMENTS**

**Final Report
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DETECTION OF REFLECTOR SURFACE FROM NEAR FIELD PHASE MEASUREMENTS

INTRODUCTION

The deviation of a reflector antenna surface from a perfect parabolic shape causes degradation of the performance of the antenna. The shape of the antenna is therefore desired for several applications. If the shape of the antenna can be determined quickly during its manufacture, localized deviations from a perfect surface might be eliminated. If an antenna should become damaged, the location of the damage may allow easier repair. This is particularly important since the damage is not easy to see and is difficult to measure directly.

The problem of determining the shape of the reflector surface in a reflector antenna using near field phase measurements is not a new one. A recent issue of the IEEE transactions on Antennas and Propagation (June, 1988) contained numerous descriptions of the use of these measurements, including works by Y Rahmat-Samii, et al, W. Chujo, et al., and J. J. Lee, et al. These accounts use one of two methods: holographic reconstruction or inverse Fourier transform.

Holographic reconstruction, used by Rahmat-Samii, makes use of measurement of the far field (amplitude and phase) of the reflector and

then applies the Fourier transform relationship between the far field and the current distribution on the reflector surface.

Inverse Fourier transformation uses the phase measurements to determine the far field pattern using the method of Kerns. After the far field pattern is established, an inverse Fourier transform is used to determine the phases in a plane between the reflector surface and the plane in which the near field measurements were taken.

These calculations are time consuming since they involve a relatively large number of operations. For the holographic reconstruction technique, the calculations are of the order of $n^2\log(2n)$ floating point operations per phase measurement. The inverse Fourier transform method requires $n^2\log(2n)$ calculations to obtain the far field pattern, followed by $n^2\log(2n)$ operations to obtain the near field phases again.

A much faster method can be used to determine the position of the reflector. This method makes use of simple geometric optics to determine the path length of the ray from the feed to the reflector and from the reflector to the measurement point. This method takes only 57 floating point operations per phase measurement and gives the specular reflection point directly, rather than the phase at a plane near the reflector, as the inverse Fourier transform method does.

For small physical objects and low frequencies, diffraction effects have a major effect on the error, and the algorithm provides incorrect results. It is believed (but not proven) that the effect is less noticeable

for large distortions such as antenna warping, and more noticeable for small, localized distortions such as bumps and depressions such as might be caused by impact damage.

Determination of the applicable distortion feature sizes is outside the scope of this work.

THE REFLECTOR SURFACE ESTIMATION ALGORITHM

Necessary assumptions.

The Reflector Surface Estimation (RSE) algorithm developed here, requires that there be no caustic points between the reflector surface and the measurement plane. If this assumption is met, each point on the phase measurement plane corresponds to either zero or one specular reflection point on the antenna surface.

Geometry of the problem.

The geometry used in the discussions throughout this document are shown in Figure 1. In accordance with normal conventions, the antenna radiates in the z-direction. A feed horn is located at the apparent focus (x_f, y_f, z_f) . A ray emitted from the feed intersects the reflector surface at the point (x, y, z) . The ray is reflected from (x, y, z) and intersects the near field plane at a point (x_a, y_a, z_a) .

Required data.

The RSE algorithm requires transform phase measurements in the near field of a reflector antenna to the point on the antenna which caused the specular reflection. Required inputs to the basic algorithm are:

Phase measurements	Absolute phase measurements or relative phase measurements which can be converted to absolute.
Frequency	The frequency at which the phase measurements were taken.
Antenna feed location	The location of the antenna feed in the coordinate system in which the results are desired.
Reference length	One physical measurement which must be made to provide relative phase length.
Phase measurement	The distance from the origin of the coordinate system to the plane in which the phase measurements are made.

Theory.

The electrical distance from the feed of the antenna to the phase measurement plane can be found from:

$$d = d_{ref} - \frac{\phi_{ref} - \phi_{ij}}{k} \quad (1)$$

The distance consists of two components: the distance from the feed to the reflector and the distance from the reflector to the measurement point.

$$d_{ij} = \sqrt{(x-x_f)^2 + (y-y_f)^2 + (z-z_f)^2} + \sqrt{(x-x_a)^2 + (y-y_a)^2 + (z-z_a)^2} \quad (2)$$

It is desired to know the location of that reflector point. Since we know the phase at many points in the near field, we can calculate the angle of arrival of the ray. The partial derivatives are:

$$\frac{\partial \phi_{ij}}{\partial x} = \frac{\phi_{i+1,j} - \phi_{i-1,j}}{x_{i+1,j} - x_{i-1,j}}, \quad \frac{\partial \phi_{ij}}{\partial y} = \frac{\phi_{i,j+1} - \phi_{i,j-1}}{y_{i,j+1} - y_{i,j-1}} \quad (3)$$

$$m_x = \frac{1}{k} \frac{\partial \phi_{ij}}{\partial x}, \quad m_y = \frac{1}{k} \frac{\partial \phi_{ij}}{\partial y}, \quad m_z = \frac{1}{\sqrt{1 - m_x^2 - m_y^2}} \quad (4)$$

From these derivatives, we can define the path of the incoming ray:

$$x = \frac{m_x}{m_z} (z - z_a) + x_a, \quad y = \frac{m_y}{m_z} (z - z_a) + y_a \quad (5)$$

We define constants representing the slopes of the lines:

$$C_1 = \frac{m_x}{m_z}, \quad C_2 = \frac{m_y}{m_z} \quad (6)$$

Substituting (5) and (6) into (2)

$$d_{ij} = \sqrt{(C_1(z - z_a) + x_a - x_f)^2 + (C_2(z - z_a) + y_a - y_f)^2 + (z - z_f)^2} + \sqrt{(x - x_a)^2 + (y - y_a)^2 + (z - z_a)^2} \quad (7)$$

or:

$$d_{ij} = \sqrt{(-C_1 z_a + x_a - x_f + C_1 z)^2 + (-C_2 z_a + y_a - y_f + C_2 z)^2 + (z - z_f)^2} + \sqrt{(x - x_a)^2 + (y - y_a)^2 + (z - z_a)^2} \quad (8)$$

Two new constants are now defined,

$$d_1 = -C_1 z_a + x_a - x_f \quad d_2 = -C_2 z_a + y_a - y_f \quad (9)$$

Substituting into equation (8)

$$d_{ij} = \sqrt{(d_1 + C_1 z)^2 + (d_2 + C_2 z)^2 + (z - z_f)^2} + \sqrt{(x - x_a)^2 + (y - y_a)^2 + (z - z_a)^2} \quad (10)$$

Expanding the first term and segregating powers of z ,

$$d_{ij} = \sqrt{(d_1^2 + 2d_1 C_1 z + C_1^2 z^2) + (d_2^2 + 2d_2 C_2 z + C_2^2 z^2) + (z^2 - 2zz_f + z_f^2)} + \sqrt{(x - x_a)^2 + (y - y_a)^2 + (z - z_a)^2} \quad (11)$$

or:

$$d_{ij} = \sqrt{(d_1^2 + d_2^2 + z_f^2) + (2d_1 C_1 + 2d_2 C_2 - 2z_f)z + (C_1^2 + C_2^2 + 1)z^2} + \sqrt{(x - x_a)^2 + (y - y_a)^2 + (z - z_a)^2} \quad (12)$$

Three additional constants are defined:

$$f_1 = d_1^2 + d_2^2 + z_f^2 \quad (13)$$

$$f_2 = 2d_1C_1 + 2d_2C_2 - 2z_f \quad (14)$$

$$f_3 = C_1^2 + C_2^2 + 1 \quad (15)$$

Substituting (13) through (15) into (8)

$$d_{ij} = \sqrt{f_1 + f_2z + f_3z^2} + \sqrt{(x-x_a)^2 + (y-y_a)^2 + (z-z_a)^2} \quad (16)$$

Substituting (6) into equation (16) yields

$$d_{ij} = \sqrt{f_1 + f_2z + f_3z^2} + \sqrt{C_1^2(z-z_a)^2 + C_2^2(z-z_a)^2 + (z-z_a)^2} \quad (17)$$

$$d_{ij} = \sqrt{f_1 + f_2z + f_3z^2} + \sqrt{f_3(z-z_a)^2} \quad (18)$$

$$\sqrt{f_1 + f_2z + f_3z^2} = d_{ij} - \sqrt{f_3(z-z_a)^2} \quad (19)$$

The second term on the right hand side of equation (19) can be either $z-z_a$ or z_a-z . One root represents the desired solution and the other root represents a point along the ray but in the positive z direction from the near field plane.

Squaring both sides and selecting the proper root,

$$f_1 + f_2z + f_3z^2 = d_{ij}^2 - 2\sqrt{f_3}(z-z_a)d_{ij} + f_3(z-z_a)^2 \quad (20)$$

Separating the powers of z ,

$$f_1 + f_2z + f_3z^2 = d_{ij}^2 - 2\sqrt{f_3}z_a d_{ij} + f_3z_a^2 + (2\sqrt{f_3}d_{ij} - 2f_3z_a)z + f_3z^2 \quad (21)$$

The z^2 terms cancel, so

$$f_1 + f_2 z = d_{ij}^2 - 2\sqrt{f_3} z_a d_{ij} + f_3 z_a^2 + (2\sqrt{f_3} d_{ij} - 2f_3 z_a)z \quad (22)$$

Solving for z ,

$$z = \frac{f_1 - d_{ij}^2 + 2\sqrt{f_3} z_a d_{ij} - f_3 z_a^2}{2\sqrt{f_3} d_{ij} - 2f_3 z_a - f_2} \quad (23)$$

The x and y points may be found from equation (5).

To obtain these results, the floating point operations in table 1 must be performed.

EFFECT OF NEAR FIELD GRID SIZE ON ACCURACY

An attempt was made to determine the effect of the near field grid size on the accuracy. The accuracy should worsen with larger grid sizes because the partial derivatives are determined from the phases of the nearest neighbors, and, in the presence of distortion, the calculated partial derivatives differs from the true local partial derivative for large grid sizes.

The analysis uses as a reflector model a parabola with cosine distortion in one of the axes. The surface is described by the equation

$$z = \frac{x^2 + y^2}{2f} + \delta \cos\left(2\pi \frac{y_{\max} - y}{y_{\max} - y_{\min}}\right)$$

with δ ranging from 0 to 0.007 meters.

The average error as a function of number of elements in the model antenna is plotted in figure 2 for several levels of distortion. As can be seen from the figure, the algorithm error varies nearly linearly with input distortion and is not greatly influenced by the element size. The invocations of RSE, and that the RSE algorithm failed for the large values of distortion for large grid sizes (evidenced by the curves which terminate early on the left of the plot). The RSE algorithm determined that some pairs of input phases were increasing or decreasing, wrote a message to the screen, and terminated the calculations for these cases.

For successful invocation of RSE, however, the accuracy of the result is not heavily influenced by grid size.

This is not to say that the number of grid points is not an important parameter. If the number of grid points is small, the position of the reflector surface will be known at only a few points.

EFFECT OF PHASE MEASUREMENT ERROR ON ACCURACY

An important performance measurement for any algorithm that uses real measurements is the effect of errors in the measurements on the accuracy of the results. In order to determine the output of the program to input noise, Gaussian noise of various amplitudes was added to the input phase measurements. The results are shown in figure 3.

The nonlinearity in the average output error as a function of input noise is apparently because the major effect on the error at low input noise levels is due to truncation errors in the algorithm. At higher levels, the error due to noise is the dominant part.

APPENDIX I

AUXILIARY PROGRAMS

This appendix contains description and listings of auxiliary programs used in the analysis. These programs include:

- vary: A program which uses all of the subroutines and functions below to produce error data based on variations in grid spacing, phase accuracy, and frequency.
- rnfpg: A subroutine which generates near field phase data on regular grid points based on user-supplied reflector distortion.
- fixphi: A subroutine which accepts the near field phase data supplied from rnfpg or from actual phase measurements and eliminates discontinuities which normally occur either at π and at $-\pi$ or at 0 and 2π . The input range is either $(-\pi, \pi)$ or $(0, \pi)$ and the output range is unlimited.
- rseerr: A subroutine which includes the RSE algorithm and uses a user-supplied reflector distortion function (also supplied in rnfpg) to determine the error of the RSE algorithm.
- reffun: A function which is supplied to rnfpg and rseerr which returns the z position of a simulated reflector surface given the x and

y coordinates. The partial derivatives with respect to x, y, and z are also given.

Subroutine RNFGP.

RNFGP theory.

Program rnfpg is an iterative procedure used to determine a point on a reflector, x_r , y_r , z_r , which will reflect incident rays from a known feed point to a known point in a near field plane. Only two of the variables are required; the third can be determined because it is known that the point lies on the reflector surface. The projection of the geometry in the $y=0$ plane is shown in figure 4.

The procedure begins with the selection of a starting value for the solution. The assumption is made that the x and y coordinates on the reflector are close to the x and y coordinates in the near field plane. About this point, four rays are used to probe the location of the exact solution. These rays originate from the feed location, intersect the reflector at four points arranged about the assumed solution (see figure 5).

Each of the rays is bounced off the reflector, following the laws of geometric optics. The intersection of the resulting ray and the near field plane is then calculated. These projections and the target grid point are shown in figure 5.

From these points, a new value of x_r, y_r is selected by linear interpolation:

$$x_r' = x_r - \delta + 2 * \delta * (x_a - x_{a3}) / (x_{a1} - x_{a3})$$

$$y_r' = y_r - \delta + 2 * \delta * (y_a - y_{a4}) / (y_{a2} - y_{a4})$$

Up to this point, we have not discussed the selection of δ . Obviously, to converge to a solution, δ must decrease with each iteration. The speed of convergence to a solution is directly related to the rate at which δ decreases. If δ is decreased too quickly, however, x_r, y_r may fall outside of the bundle of rays. This is usually not fatal, if the function is well behaved, but if it happens too often, divergence may occur.

The parameter which will determine how quickly δ can be reduced is related to the linearity of the mapping from the reflector position to the near field position. If the mapping is totally linear (e.g., no distortion), only one iteration is necessary. The more non-linearity, the more iterations will be needed.

One rough indication of linearity can be obtained from the points already calculated. If the transformation were totally linear, the distance in the x axis from x_{a1} to x_{a2} would be the same as the distance in the x direction x_{a4} to x_{a3} . Using the difference between the two distances divided by the total distance from x_{a1} to x_{a3} as the measure of non-linearity, we have:

$$\text{skew}_x = |(x_{a1} + x_{a3} - x_{a2} - x_{a4}) / (x_{a1} - x_{a3})|$$

A similar measure can be made in the y direction.

$$\text{skew}_y = |(y_{a1} + y_{a3} - y_{a2} - y_{a4}) / (y_{a1} - y_{a3})|$$

The program uses the non-linearity as the basis for the decrease in the spread of the packet of rays. The program starts with a δ of 10% of the largest dimension of the antenna. After the first iteration, δ is calculated from

$$\delta_{n+1} = \delta_n * (\text{skew}')$$

Where

$$\text{skew}' = \max(0.1, \min(0.9, \max(\text{skew}_x, \text{skew}_y)))$$

The maximum value of skew_x or skew_y is used, so long as that value is greater than 0.1 and less than 0.9.

After the new value for δ is determined, a new bundle of rays is launched. A test is made to determine if the bundle of rays does enclose the solution. This can be determined by examining the intersection of the rays with the near field plane. x_{a3} should be less than x_a and x_{a1} should be greater than x_a , with similar requirements in the y axis. If one of these conditions is not met, an informative message is sent to the console and the value of δ is automatically multiplied by 2. The iteration then continues.

After each iteration, a test is made to determine if the error in the near field plane has converged to within the maximum error used in the program's calling argument. If it has, the value is printed out to a file and the program continues with the next point in the near field plane.

Subroutine fixphi.

Subroutine fixphi takes as its input the results of rnfpg of near field phase measurements from an antenna facility and transforms the relative phase measurements ($-\pi < \phi < \pi$) or ($0 < \phi < 2\pi$) to measurements which can be used to determine phase length. For example, if the following line were input into the program:

1.0 1.5 2.5 0.5 1.5

the program would convert the line to:

1.0 1.5 2.5 3.64159 4.64159

The program works by first examining the data to see if it meets one of the conditions: ($-\pi < \phi < \pi$) or ($0 < \phi < 2\pi$). If it meets neither condition, an error message is displayed on the console and the program terminates. If either condition is met, the program continues.

The program continues by rewriting the input file and reading input while processing and printing the output. The first input value is special in that its value is always preserved. After the first value, each

measurement is examined to determine if it appears that the data has gone through a transition from $-\pi$ to π or from 2π to 0.

RNFPG performance.

There were two figures of merit of the routine which were traded against each other to obtain maximum performance: computational speed and accuracy. Because of the iterative nature of the algorithm, additional accuracy can always be obtained by allowing more time for the computations, up to the precision limits of the machine. Double precision numbers were used as the default for the algorithm to limit the effect of machine precision on the output.

Required accuracy is an argument in the invocation of RNFPG, and the algorithm will execute until that accuracy is obtained.

In order to determine the effect of accuracy on expected execution time, number of iterations was plotted as a function of required accuracy. The results are shown in figure 6.

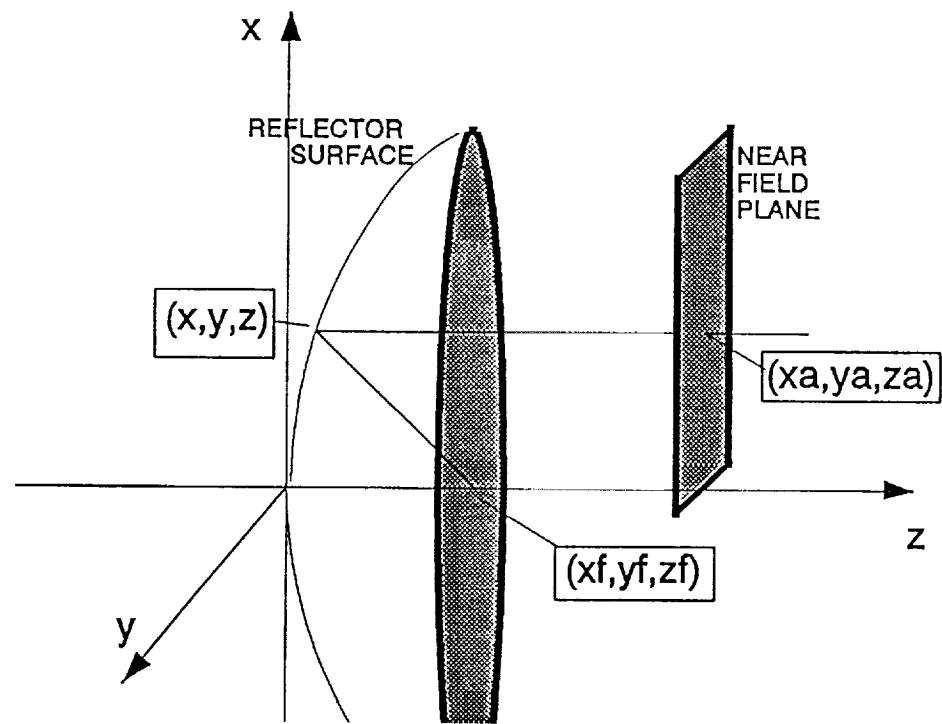


Figure 1. Geometry used to develop the RSE algorithm

Table1. Operations and timing. Times shown are for a Motorola 68881 co-processor operating at 40 mHz. Time is given in microseconds.

	ADD	SUBTRACT	MULTIPLY	DIVIDE	SQ.ROOT	TOTAL
$\partial\phi/\partial x$		2		1		3.0
$\partial\phi/\partial x$		2		1		3.0
m_x				1		1.0
m_y				1		1.0
m_z		2	2	1	1	6.0
C_1				1		1.0
C_2				1		1.0
d_1	1	1	1			3.0
d_2	1	1	1			3.0
f_1	2		3			5.0
f_2	1	1	3			5.0
f_3	2		2			4.0
z	1	4	9	1	2	17.0
x	1	1	1	1		4.0
Total	9.0	14.0	22.0	9.0	3.0	57.0
Cycle/oper	51	51	71	103	107	
Total cycles	459.0	714.0	1,562.0	927.0	321.0	2,100.0
Time/cycle	0.025	0.025	0.025	0.025	0.025	
Total time	11.48	17.85	0.00	23.18	0.00	52.51

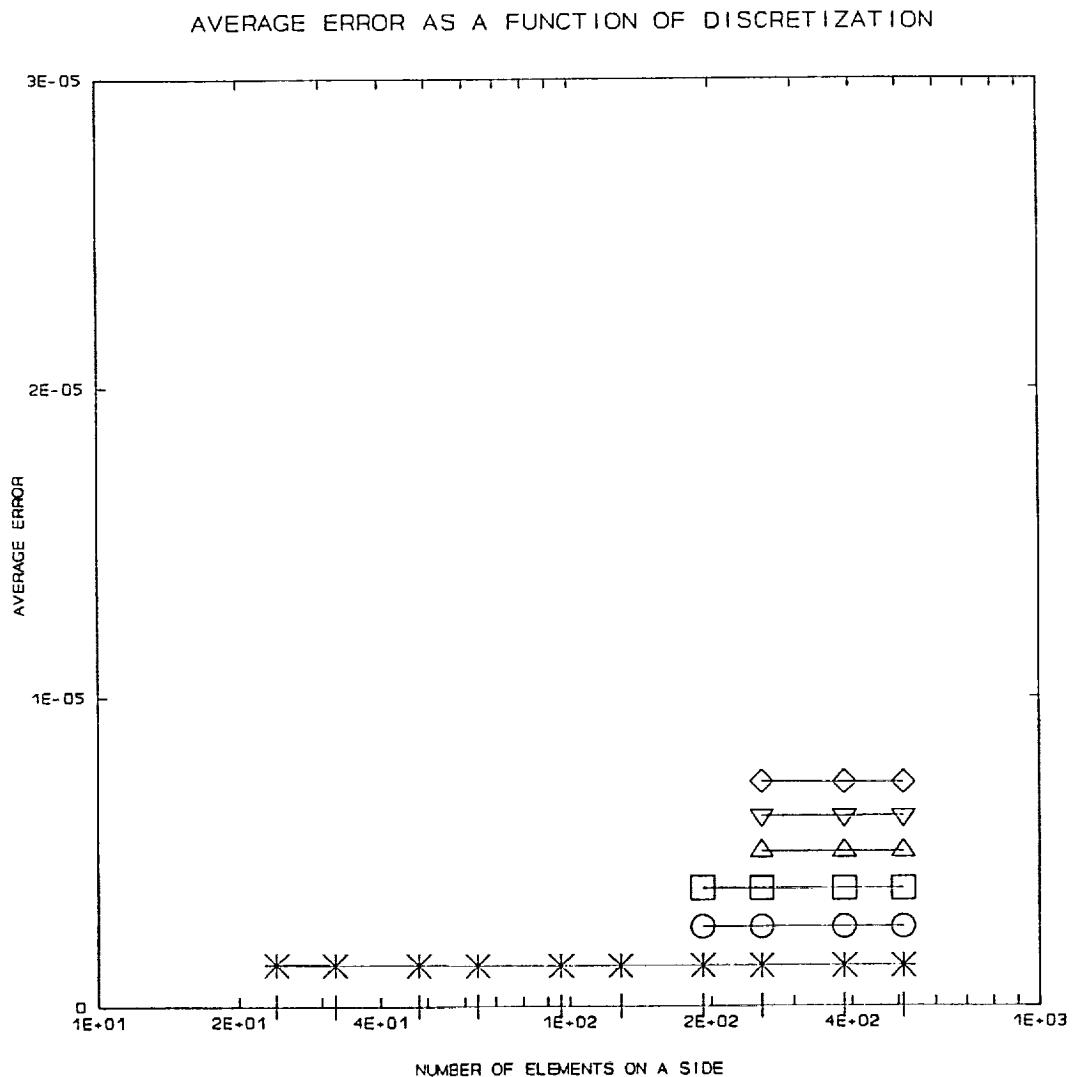


Figure 2. Error vs. Discretization. Curves are (from bottom) for 1, 2, 3, 4, 5, and 6mm distortion.

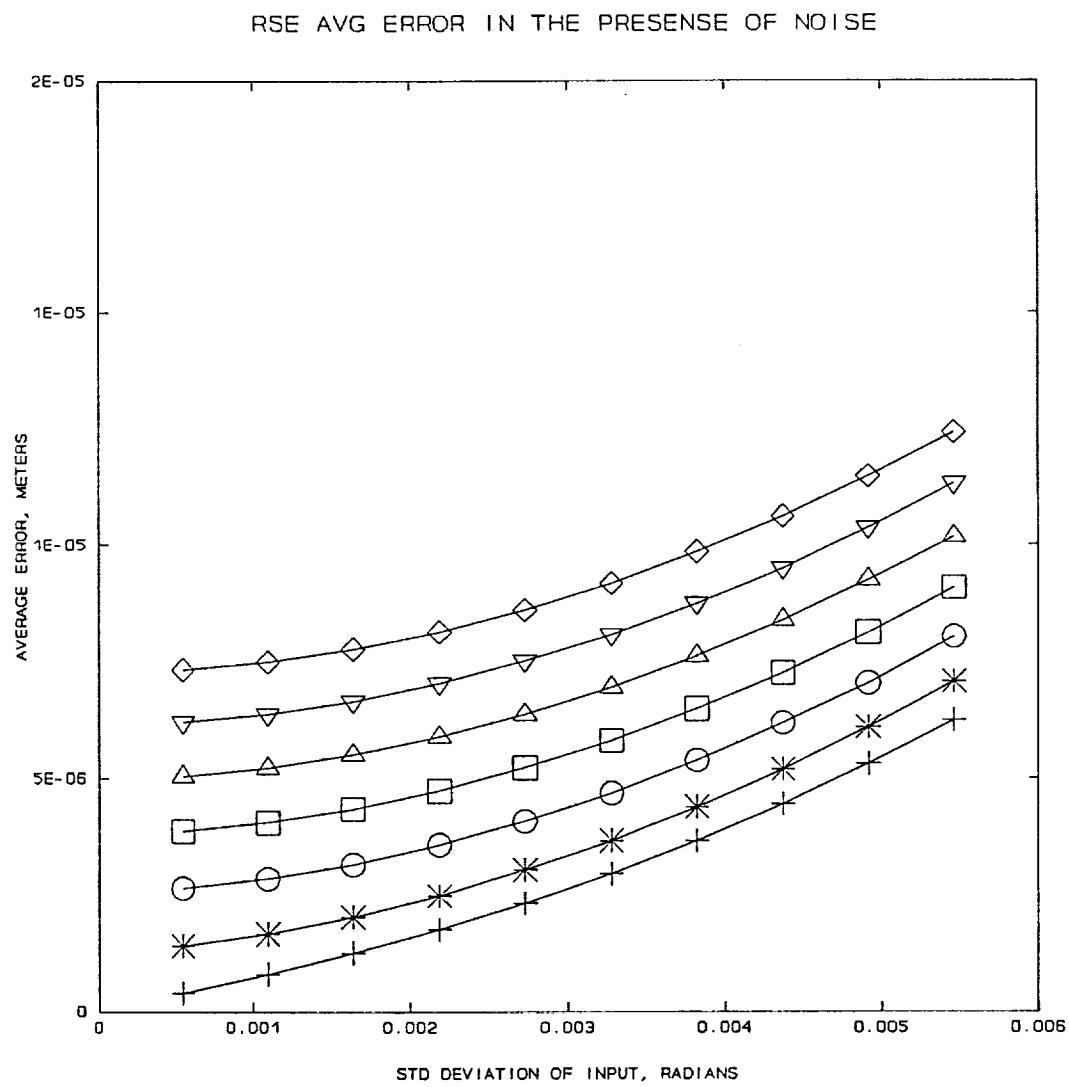


Figure 3 RSE error in the presence of noise. Curves are (from bottom) for 1, 2, 3, 4, 5, and 6mm distortion

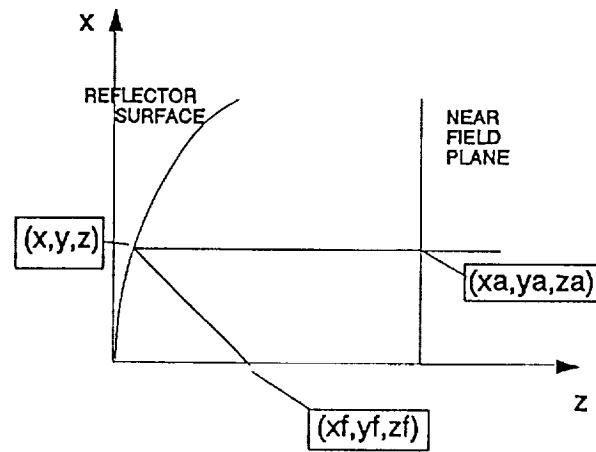


Figure 4. Problem geometry in the plane $y=0$

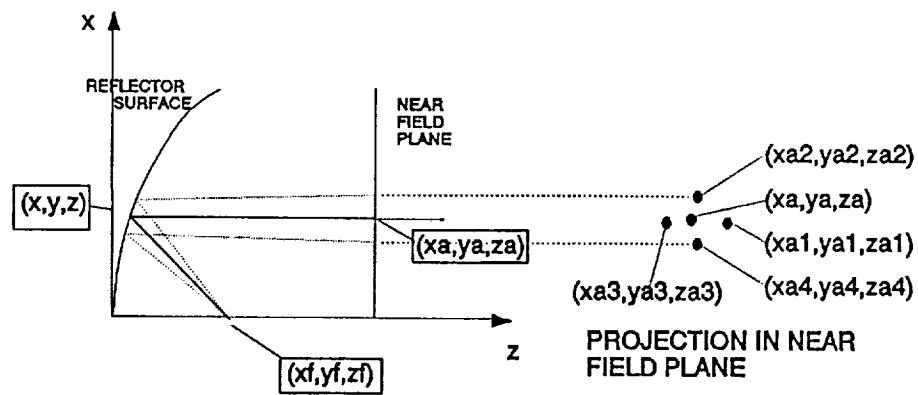


Figure 5.rnfpq ray tracing

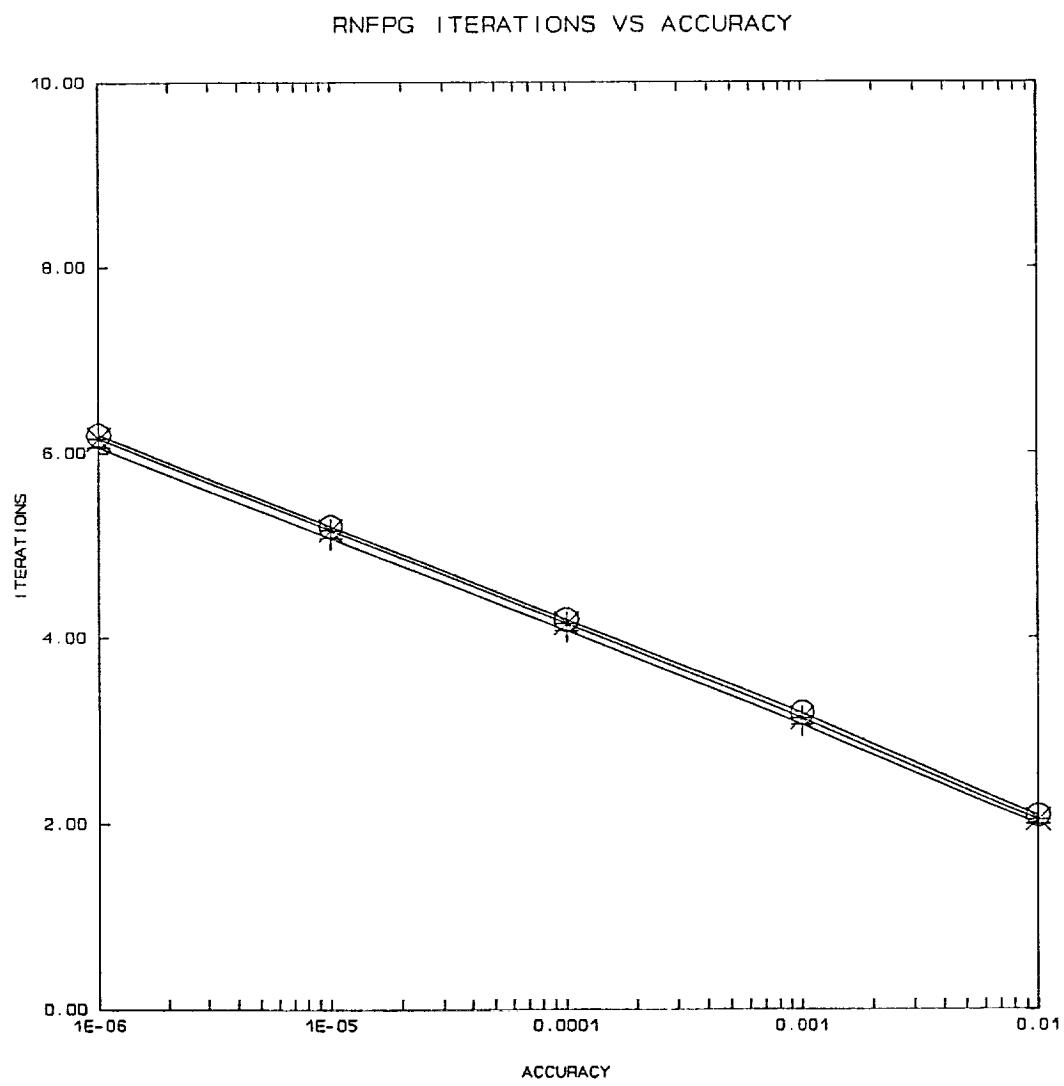


Figure 6. rnfpq iterations versus accuracy. Curves are (from bottom) for 1, 2, and 3mm distortion.

COMPUTER PROGRAM LISTINGS

The programs used with this algorithm are listed on the following pages.

vary.f

```
c      vary.f compiles into a variety of programs depending on
c      the mode of compilation
c      Compilation must be done with the c preprocessor cpp.
c      One of the following may be defined
c
c          (none)           defaults to vary number of cells
c          ERROR           varies the allowable error of rnfpq
c
c
program vary
implicit double precision (a-h)
implicit double precision (o-z)
double precision xamp(8),yamp(8)
common /partial/ pdfdx,pdfdy,pdfdz
common /distort/ del,omega,xampl,yampl
integer type
common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
real maxerr(20,20),avgerr(20,20),rmserr(20,20)
integer error(20,20)
integer npts(8),nerrors(8)
#define MAX_CURVES 8
#define MAX_POINTS 50
#ifndef ERROR
    character*80 filename,plttl,xttl,yttl,zttl
    real xdata(50,8)
    real ydata(50,8)
    real avgitr
    common /perf/ avgitr
#else ERROR
    real xdata(50,8)
    real adata(50,8)
    real rdata(50,8)
    real mdata(50,8)
    real sigma(50,8)
    real inacc(50,8)
#endif ERROR
common /plot/ idist,igrid,
1 maxerr(20,20),avgerr(20,20),rmserr(20,20),error(20,20)
data xamp /0.00, 0.01, 0.02, 0.03, 0.04, 0.05, 0.06, 0.07/
data yamp /0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00/
fmaxerr=.000001
ymax=1.1
ymin=0.1
xmax=0.5
xmin=-0.5
type = 1
#ifndef ERROR
    infile1=513
#else
    infile1=512
    infile2=(infile1*3)/4
    idiv = ifix(log(float(infile1))/log(2.0)-2.5)
    ngrids =2*ifix(log(float(infile1))/log(2.0)-2.5)
    infile1=infile1+1
    infile2=infile2+1
#endif ERROR
f = 1.0
xf = 0.0
```

vary.f

```
      yf = 0.0
      zf = 1.0
      zp = 1.0
      periods = 1.0
      omega = 2.0 * 3.14159265 * periods / (ymax-ymin)
      freq=30500000000.
      c
      Wave number
      k = 2.0 * 3.141592650 / (300000000/freq)

      open(7,file="results.dat")
      open(99,file="contour.dat")
      min_dist=1
      max_dist=7
      do 10 i=min_dist,max_dist
      idist=i
      xampl=xamp(i)
      yampl=yamp(i)
      write(7,105)
105   format('avgerr.wpg')
      write(7,106) xampl,yampl
106   format(' rnfpg error analysis'/
1      ' amplitude of (x,y) distortion = ('/
2      ',d18.10,',',d18.10,')' )

      xlambd = 0.1
      t = xampl
      del = t * xlambd

#define ERROR
      do 20 ierror=1,5
      ferrmax=.000001*(10**(ierror-1))
      write(6,*)"max err = ",ferrmax
      write(7,*)"max err = ",ferrmax
      open(4,file="ph1.dat",form='UNFORMATTED')
      call rnfpg(infile1,ferrmax)
      close(4)
      xdata(ierror,i) = ferrmax
      ydata(ierror,i) = avgitr
20      continue
      npts(i) = ierror-1
10      continue
      filename = "iter2.wpg"
      pltttl = "RNFPG ITERATIONS VS ACCURACY"
      xtll = "ACCURACY"
      yttl = "ITERATIONS"
      zttl = "DISTORTION"
      call plotwpg(filename,pltttl,xttl,yttl,zttl,
1      .000001,.01,.001,0.,10.,2.,1,0,
2      max_dist-min_dist+1,
2      npts,xdata,ydata)
#else
      open(4,file="ph1.dat",FORM='unformatted')
      call rnfpg(infile1,fmaxerr)
      close(4)
      open(3,file="ph1.dat",FORM='unformatted')
      open(4,file="ph1f.dat",FORM='unformatted')
      call fixphi(infile1)
      close(4)
      close(3)
```

vary.f

```
open(4,file="ph2.dat",FORM='unformatted')
call rnfpq(infile2,fmaxerr)
close(4)
open(3,file="ph2.dat",FORM='unformatted')
open(4,file="ph2f.dat",FORM='unformatted')
call fixphi(infile2)
close(4)
close(3)

igrid=0
do 20 j=1,idiv
    igrid=igrid+1
    xdata(igrid,i) = infile1/(2**((j-1))
    open(4,file='ph1f.dat',FORM='unformatted')
    call rsegrid(infile1,1+(infile1-1)/(2**((j-1)))
    adata(igrid,i)=avgerr(igrid,i)
    mdata(igrid,i)=maxerr(igrid,i)
    rdata(igrid,i)=rmserr(igrid,i)
    if(error(igrid,i).ne.0)go to 21
    close(4)
    igrid=igrid+1
    xdata(igrid,i)=infile2/(2**((j-1))
    open(4,file='ph2f.dat',FORM='unformatted')
    call rsegrid(infile2,1+(infile2-1)/(2**((j-1)))
    adata(igrid,i)=avgerr(igrid,i)
    mdata(igrid,i)=maxerr(igrid,i)
    rdata(igrid,i)=rmserr(igrid,i)
    if(error(igrid,i).ne.0)go to 21
    close(4)
20    continue
21    npts(i) = j-1

do 30 j=1,10
    nerrors(j) = 10
    sigma(j,i)=((300000000./freq)/(360.*.01*5.)*float(j))
    open(4,file='ph1f.dat',FORM='unformatted')
    rewind(4)
    call rseerr(infile1,sigma(j,i),inacc(j,i),ierrflg)
    close(4)
30    continue
10    continue

call plotwpg("maxerr.wpg",
1 "MAXIMUM ERROR AS A FUNCTION OF DISCRETIZATION",
2 "NUMBER OF ELEMENTS ON A SIDE","MAXIMUM ERROR","DISTORTION",
3 10.,1000.,10.,0.,.00003,.00001,1,0,
4 max_dist-min_dist+1,
5 npts,xdata,mdata)

call plotwpg("avgerr.wpg",
1 "AVERAGE ERROR AS A FUNCTION OF DISCRETIZATION",
2 "NUMBER OF ELEMENTS ON A SIDE","AVERAGE ERROR","DISTORTION",
3 10.,1000.,10.,0.,.00003,.00001,1,0,
4 max_dist-min_dist+1,
5 npts,xdata,adata)

call plotwpg("rmserr.wpg",
1 "ROOT MEAN SQUARE ERROR AS A FUNCTION OF DISCRETIZATION",
2 "NUMBER OF ELEMENTS ON A SIDE","RMS ERROR","DISTORTION",
1 10.,1000.,10.,0.,.00003,.00001,1,0,
2 max_dist-min_dist+1,
3 npts,xdata,rdata)

call plotwpg("randerr.wpg",
```

vary.f

```
1 "RSE AVG ERROR IN THE PRESENCE OF NOISE",
2 "STD DEVIATION OF INPUT, RADIANS","AVERAGE ERROR, METERS",zttl,
3 0.,.006,.001,0.,.00002,.00005,0,0,
4 max_dist-min_dist+1,
5 nerrors,sigma,inacc)

#endif  ERROR
stop
end
```

reffun.f

```
c      Calculate the z coordinate of the reflector surface
      real*8 function reffun(x,y)

      implicit real*8 (a-h)
      implicit real*8 (o-z)
      real argx, sinfunx, cosfunx
      real argy, sinfuny, cosfuny
      integer type
      real*8 x,y,f,del,omega,ymax
      real*8 temp

      common /partial/ pdfdx,pdfdy,pdfdz
      common /distort/ del,omega
      common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type

c      x and y are the x and y positions of the point
c      del is the distortion amplitude factor
c      omega is the distortion wave number
c      ymax is the maximum y value

      if(type .eq. 1) then
c      This type is for an antenna with sinusoidal distortion that varies
c      only with the y variable

          argy = omega * (ymax-y)
          sinfuny = sin(argy)
          cosfuny = cos(argy)
          temp = -0.5/f
          pdfdx = x*temp
          pdfdy = y*temp - del * omega * sinfuny
          pdfdz = 1.0
          reffun = (x**2+y**2)/(4.0*f)+del*cosfuny
          return
      else if (type .eq. 2 ) then
c      This type is for an antenna with sinusoidal distortion that varies
c      only with the x variable

          argx = omega * (xmax-x)
          sinfunx = sin(argx)
          cosfunx = cos(argx)
          temp = -0.5/f
          pdfdx = x*temp - del * omega * sinfunx
          pdfdy = y*temp
          pdfdz = 1.0
          reffun = (x**2+y**2)/(4.0*f)+del*cosfunx
          return
      else if (type .eq. 3 ) then
c      This type is for an antenna with sinusoidal distortion that varies
c      with both the x and the y variable

          argx = omega * (xmax-x)
          argy = omega * (ymax-y)
          sinfunx = sin(argx)
          cosfunx = cos(argx)
          temp = -0.5/f
          pdfdx = x*temp - del * omega * sinfunx
          pdfdy = y*temp - del * omega * sinfuny
          pdfdz = 1.0
          reffun = (x**2+y**2)/(4.0*f)+del*cosfunx +del*cosfuny
          return
      endif
      end
```

rnfpg.f

```
subroutine rnfpg(nphasegp,ferrmax)
c   The purpose of this program is to detect an antenna
c   reflector surface from the near field phase distribution.
c   The near field phase distribution is defined on an nxn
c   rectangular grid system.
c   Feeder location(xf,yf,zf), value of lambda, diameter of
c   the reflector aperture(d)
c*****
implicit real*8 (a-h)
implicit real*8 (o-z)
real*8 xa, ya
real avgitr
common /partial/ pdfdx,pdfdy,pdfdz
integer type
common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
common /perf/ avgitr
dimension phi(1026)
open(11,file='res')
pi = 3.1415926
c   Diameter of the region of interest on the reflector
d=1.
c   Near field grid spacing
delfn = d/(nphasegp-1)
k = 2*3.1415926 /(300000000. / freq)
fctrmin = 0.1
fctrmax = 0.9
nfirst=1
      write(6,998)ferrmax
998  format("max err =",g8.3)
nloops=0
c   Scan through the x axis of the near field
do 10 i=1,nphasegp
      call tick(i)
c   Scan through the y axis of the near field
do 20 j=1,nphasegp
      Define the x,y,z  coordinates in the near field
      xa = xmin + delfn * (i-1)
      ya = ymin + delfn * (j-1)
      za = zp
      set up for search in reflector plane
      xr=xa
      yr=ya
      delta=dmax1(dabs(xmax-xmin),dabs(ymax-ymin))/10.
      reflector plane iteration loop
c
c
601      continue
      nloops=nloops+1
c
c   launch four rays
      call qray(xr+delta,yr,xa1,ya1)
      call qray(xr,yr+delta,xa2,ya2)
      call qray(xr-delta,yr,xa3,ya3)
      call qray(xr,yr-delta,xa4,ya4)
```

rnfpg.f

```
if(xa3.gt.xa)goto 649
if(xa.gt.xa1)goto 649
if(ya4.gt.ya)goto 649
if(ya.gt.ya2)goto 649
go to 650

649      continue
write(6,648)
format(' got outside of bundle of rays')
delta=delta*2
goto 601

650      continue
if(xa1.ne.xa3)
1      xr=2*delta/(xa1-xa3)*(xa-xa3) + xr - delta
if(ya2.ne.ya4)
1      yr=2*delta/(ya2-ya4)*(ya-ya4) + yr - delta
continue

skewx = 0
skewy = 0
if((xa1 - xa3) .eq. 0)goto 680
skewx = dabs(((xa1+xa3)-(xa2+xa4))/(xa1-xa3))
680      if((ya2 - ya4) .eq. 0)goto 681
skewy = dabs(((ya2+ya4)-(ya1+ya3))/(ya2-ya4))
681      factor=2*dmax1(skewx,skewy)
factor=dmax1(fctrmin,factor)
factor=dmin1(fctrmax,factor)

delta=delta*factor
if((abs((xa1-xa3)*pdfdx)+abs((ya2-ya4)*pdfdy))
1      .gt.ferrmax) goto 601
zr=reffun(xr,yr)
dist=dsqrt((xf-xr)**2+(yf-yr)**2+(zf-zr)**2)+dsqrt((xa-xr)**2+(ya-yr)**2+(za-zr)**2)
phi(j)=k*dist
nphi=phi(j)/(2*pi)
phi(j)=phi(j)-nphi*2*pi
if(nfirst.ne.1)goto 200
write(4)dist,phi(j)
199      format(f14.8/f14.8)
nfirst=0
200      continue

20      continue
write(4)(phi(j),j=1,nphasegp)
555      format(1026f14.8)
10      continue
close(11)
avgitr = float(nloops)/float(nphasegp**2)
write(7,997)avgitr
write(6,997)avgitr
997 format("avg iter = "f8.3)
return
end

subroutine qray(xr,yr,xa,ya)
implicit real*8 (a-h)
implicit real*8 (o-z)
common /partial/ pdfdx, pdfdy, pdfdz
integer type
common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
```

rnfpq.f

```
real*8 l1x, l2x, l1y, l2y, l1z, l2z
zr = reffun(xr,yr)
l1x = xf - xr
l1y = yf - yr
l1z = zf - zr
absnrm1 = pdfdx**2 + pdfdy**2 + pdfdz**2
r = 2.0*(pdfdx * l1x + pdfdy * l1y + pdfdz * l1z)/absnrm1
l2x = l1x - r * pdfdx
l2y = l1y - r * pdfdy
l2z = l1z - r * pdfdz
quick = (zp-zr)/l2z
xa = quick * l2x + xr
ya = quick * l2y + yr
return
end
```

fixphi.f

```
subroutine fixphi(ninfile)
implicit double precision (a-h)
implicit double precision (o-z)
double precision phi(1026)

pi = 3.14159265
twopi = 2*3.14159265

read(3)dref,phiref
write(4)dref,phiref
199 format(f14.8/f14.8)
    ifirst = 1
    irow = 0

    do 10 i=1,ninfile
        read(3)(phi(n),n=1,ninfile)
        if(ifirst .eq. 1) phirow = phi(1)
        ifirst = 0
        philast = phirow
        if((phi(1)-phirow) .lt. (-1*pi)) then
            irow = irow + 1
            philast=phi(1)
            phirow=phi(1)
        else if((phi(1)-phirow) .gt. pi) then
            irow = irow - 1
            philast=phi(1)
            phirow=phi(1)
        endif
        icol = irow
        do 20 j=1,ninfile
            if((phi(j)-philast) .lt. (-1*pi)) then
                icol = icol + 1
            else if((phi(j)-philast) .gt. pi) then
                icol = icol - 1
            endif
            philast=phi(j)
            phi(j) = phi(j) + icol*twopi
            continue
20      write(4)(phi(n),n=1,ninfile)
        continue
10      continue
7 format(1026f14.0)
8 format(1026f14.8)
return
end
```

rseggrid.f

```
subroutine rseggrid(ninfile,ntouse)
c
c   the purpose of this program is to detect an antenna reflector
c   surface from the near field phase distribution. The near field
c   phase distribution is defined on an nxn rectangular grid system
c
c   surface detection
c   implicit double precision (a-h)
c   implicit double precision (o-z)
c   double precision lambda,mx,my,mz,k
c   double precision phi(3,1026)
c   double precision dummy(1026)
c   real*8 reffun
c   integer contour(1026)
c   common /partial/ pdfdx,pdfdy,pdfdz
c   common /distort/ del,omega,xampl,yampl
c   integer type
c   common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
c   real maxerr(20,20),avgerr(20,20),rmserr(20,20)
c   integer error(20,20)
c   common /plot/ idist,igrid,
c   1 maxerr(20,20),avgerr(20,20),rmserr(20,20),error(20,20)
c   character*4 comment

c   error(igrid,idist)=0
c   comment = ' '
c   errmax = 0.
c   sumerr = 0.
c   sumsq = 0.
c   nsum = 0

c   if(ntouse.lt.100) write(99,801)ntouse,idist
801  format(' e',i4.4,i2.2,'.dat')
c   if(ntouse.lt.100) write(99,802)ntouse,del
802  format(' ALGORITHM ERROR WITH ',i4.4,' GRIDS AND ',
c   1 F9.3,' MM MAX SIN DISTORTION')
c
c   if(ntouse.lt.100) write(99,803)1,'err<.00003'
c   if(ntouse.lt.100) write(99,803)2,'err<.00002'
c   if(ntouse.lt.100) write(99,803)3,'err<.00001'
c   if(ntouse.lt.100) write(99,803)4,'err<.00000'
c   if(ntouse.lt.100) write(99,803)5,'err>.00000'
c   if(ntouse.lt.100) write(99,803)6,'err>.00001'
c   if(ntouse.lt.100) write(99,803)7,'err>.00002'
c   if(ntouse.lt.100) write(99,803)8,'err>.00003'
803  format(' ',i3,' ',a)
c
c   if(ntouse.lt.100) write(99,804)ntouse-2
804  format(' ',i3)
c
c   za = zp
c
c   pi = 3.14159265
c
c   read(4)dref,phiref
c
c   lambda=300000000./freq
c   k = (2*pi)/lambda
c   delx=(xmax-xmin)/(ntouse-1)
c   dely=(ymax-ymin)/(ntouse-1)
c
c   ntoskip=(ninfile/(ntouse-1))-1
c   write(6,*)' ntoskip = ',ntoskip
c
c   read in two lines of input to start the process
```

rsegred.f

```
if(ntoskip.eq.0) then
  read(4)(phi(2,n),n=1,ntouse)
else
  read(4)phi(2,1),
  1 ((dummy(iskip),iskip=1,(ntoskip)),phi(2,n),n=2,ntouse)
endif

  if(ntoskip.ne.0) then
    do 880 iskip=1,(ntoskip)
  880  read(4)dummy(1)
  endif

  if(ntoskip.eq.0) then
    read(4)(phi(3,n),n=1,ntouse)
  else
    read(4)phi(3,1),
    1 ((dummy(iskip),iskip=1,(ntoskip)),phi(3,n),n=2,ntouse)
  endif

  if(ntoskip.ne.0) then
    do 881 iskip=1,ntoskip
  881  read(4)dummy(1)
  endif

  do 400 n=1,ntouse
  400 phi(2,n)=phi(2,n)-phiref
  phi(3,n)=phi(3,n)-phiref
  do 10 i=2,ntouse-1
  c      write(7,*)
  c      xa=xmin+(i-1)*delx
  c      prepare to read in a new row
  do 11 i1=1,ntouse
  11      phi(1,i1)=phi(2,i1)
  phi(2,i1)=phi(3,i1)

  if(ntoskip.eq.0) then
    read(4)(phi(3,n),n=1,ntouse)
  else
    read(4)phi(3,1),
    1 ((dummy(iskip),iskip=1,(ntoskip)),phi(3,n),n=2,ntouse)
  endif

  if(ntoskip.ne.0.and.i.ne.(ntouse-1)) then
  882    do 882 iskip=1,ntoskip
  read(4)dummy(1)
  endif

  do 401 n=1,ntouse
  401 phi(3,n)=phi(3,n)-phiref
  do 20 j=2,ntouse-1
  ya=ymin+(j-1)*dely
  d=dref+1/k*(phi(2,j))
  c      dref and phiref are measured quantities

  dphidx=phi(3,j)-phi(1,j)
  if(dphidx.gt.pi)dphidx=dphidx-2*pi
  if(dphidx.lt.(-1*pi))dphidx=dphidx+2*pi
  if((dphidx.lt.-1).or.(dphidx.gt.1))then
    if(error(igrid,idist).eq.0)then
      error(igrid,idist)=1
      comment=' ?? '
      write(6,570)
```

rsegrid.f

```
      endif
      endif
570      format(' grid size too large')
      dphidx=dphidx/(2*delx)

      dphidy=phi(2,j+1)-phi(2,j-1)
      if(dphidy.gt.pi)dphidy=dphidy-2*pi
      if(dphidy.lt.(-1*pi))dphidy=dphidy+2*pi
      if((dphidy.lt.-1).or.(dphidy.gt.1))then
          if(error(igrid,idist).eq.0)then
              error(igrid,idist)=1
              comment=' ?? '
              write(6,570)
          endif
      endif
      dphidy=dphidy/(2*dely)
      mx = dphidx/k
      my = dphidy/k
      mz = dsqrt (1.0-mx**2-my**2)
      c1 = mx/mz
      c2 = my/mz
      d1 = -c1*za + xa - xf
      d2 = -c2*za + ya - yf
      f1 = d1**2 + d2**2 + zf**2
      f2 = 2.0 * (d1*c1 + d2*c2 - zf)
      f3 = c1**2 + c2**2 + 1.0

      znu = -f1 + (f3*za**2 - 2.0 * dsqrt(f3)*d*za
      + d**2)
      znd = (f2 + f3*2.0*za - 2.0 * dsqrt(f3)*d)
      z=znu/znd
      x=c1*(z-za) + xa
      y=c2*(z-za) + ya
      write(6,991)x,y,z
      format(" x= ",f18.10," , y= ",f18.10, " , z= ",f18.10)
      err = z - reffun(x,y)
      if(err.gt.0)then
          contour(j)=5
          if(err.gt..0001)contour(j)=6
          if(err.gt..0002)contour(j)=7
          if(err.gt..0003)contour(j)=8
      else
          contour(j)=4
          if(err.lt. -.0001)contour(j)=3
          if(err.lt. -.0002)contour(j)=2
          if(err.lt. -.0003)contour(j)=1
      endif
      derror= dabs(err)
      write(6,556)x,y,z,derror
      format(5f14.8)
      556      if(derror .gt. errmax) errmax=derror
      sumerr = sumerr + derror
      sumsq = sumsq + derror**2
      nsum = nsum + 1
      20      continue
      if(ntouse.lt.100) write(99,819)(contour(j), j=2,ntouse-1)
819      format(1026i1);
      10      continue
      rms = dsqrt(sumsq/nsum)
      average = sumerr/nsum
      maxerr(igrid,idist)=errmax
      avgerr(igrid,idist)=average
      rmserr(igrid,idist)=rms
      write(7,557)errmax,average,rms
      557      format(' maxerr = ', d14.8,
      1 ' sumerr/n = ', d14.8,
      2 ' sumsq/n = ', d14.8)
      write(7,558)ntouse,average
      558      format(' ',i4,' ',f14.8)
      return
      end
```

rseerr.f

```
subroutine rseerr(ninfile,sigma,inacc,error)
c
c      surface detection
      implicit double precision (a-h)
      implicit double precision (o-z)
      real sigma, inacc,gasdev
      integer error
      double precision lambda,mx,my,mz,k
      double precision phi(3,1026)
      real*8 reffun
      common /partial/ pdfdx,pdfdy,pdfdz
      common /distort/ del,omega,xampl,yampl
      integer type
      common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
      logical exist,opened
      integer ios,nr
      integer arg1,arg2,arg3,arg4,arg5

1 continue
      error=0.
      errmax = 0.
      sumerr = 0.
      sumsq = 0.
      nsum = 0
      za = zp

      pi = 3.14159265
      read(4,end=699,err=698)dref,phiref
      lambda=300000000./freq
      k = (2*pi)/lambda
      delx=(xmax-xmin)/(ninfile-1)
      dely=(ymax-ymin)/(ninfile-1)
c      read in two lines of input to start the process
c      read(4,end=699,err=698)(phi(2,n),n=1,ninfile)
      read(4,end=699,err=698)(phi(3,n),n=1,ninfile)

      do 400 n=1,ninfile
          perturb = sigma * gasdev()
          phi(2,n)=phi(2,n)-phiref + perturb
          perturb = sigma * gasdev()
          phi(3,n)=phi(3,n)-phiref + perturb
400 continue

      do 10 i=2,ninfile-1
          xa=xmin+(i-1)*delx
c          prepare to read in a new row
          do 11 i1=1,ninfile
              phi(1,i1)=phi(2,i1)
11          phi(2,i1)=phi(3,i1)
          read(4,end=699,err=698)(phi(3,n),n=1,ninfile)

          do 401 n=1,ninfile
              perturb = sigma * gasdev()
              phi(3,n)=phi(3,n)-phiref + perturb
401      continue
          do 20 j=2,ninfile-1
              ya=ymin+(j-1)*dely
```

rseerr.f

```
d=dref+1/k*(phi(2,j))
c
dphidx=phi(3,j)-phi(1,j)
if(dphidx.gt.pi)dphidx=dphidx-2*pi
if(dphidx.lt.(-1*pi))dphidx=dphidx+2*pi
if((dphidx.lt.-1).or.(dphidx.gt.1))then
    if(error.eq.0)then
        error=1
        write(6,510)
        format('grid size too large')
    endif
endif
dphidx=dphidx/(2*delx)

dphidy=phi(2,j+1)-phi(2,j-1)
if(dphidy.gt.pi)dphidy=dphidy-2*pi
if(dphidy.lt.(-1*pi))dphidy=dphidy+2*pi
if((dphidy.lt.-1).or.(dphidy.gt.1))then
    if(error.eq.0)then
        error=1
        write(6,510)
    endif
endif
dphidy=dphidy/(2*dely)
mx = dphidx/k
my = dphidy/k
mz = dsqrt (1.0-mx**2-my**2)
c1 = mx/mz
c2 = my/mz
d1 = -c1*za + xa - xf
d2 = -c2*za + ya - yf
f1 = d1**2 + d2**2 + zf**2
f2 = 2.0 * (d1*c1 + d2*c2 - zf)
f3 = c1**2 + c2**2 + 1.0
znu = -f1 + (f3*za**2 - 2.0 * dsqrt(f3)*d*za
        + d**2)
znd = (f2 + f3*2.0*za - 2.0 * dsqrt(f3)*d)
z=znu/znd
x=c1*(z-za) + xa
y=c2*(z-za) + ya
err = z - reffun(x,y)
derror= dabs(err)
if(derror .gt. errmax) errmax=derror
sumerr = sumerr + derror
sumsq = sumsq + derror**2
nsum = nsum + 1
20    continue
819  format(1026i1);
10    continue
rms = dsqrt(sumsq/nsum)
average = sumerr/nsum
inacc = average
write(7,555)sigma,inacc,errmax,average,rms
555 format('sigma=',g14.8,',inacc=',g14.8,',errmax=', g14.8,
1 ',average=', d14.8,',rms= ', d14.8)
write(6,557)sigma,inacc
557 format('sigma=',g14.8,',inacc=',d14.8)
write(7,558)ninfile,average
558 format(' ',i4,' ',f14.8)
return
698  write(6,*)"---error---"
      return
699  write(6,*)"---end---"
      call ERRSNS(arg1,arg2,arg3,arg4,arg5)
      write(6,*)arg1,arg2,arg3,arg4,arg5
      inquire(4,EXIST=exist,NEXTREC=nr,IOSTAT=ios,OPENED=opened)
      write(6,*)"exist",exist,"iostat",ios,"opened",opened
      write(6,*)"next record = ",nr
      write(6,*)"n=",n,"nsum=",nsum,"i=",i
      call flush(6)
      rewind (4)
      goto 1
end
```

Vctr.f

```

      program vctr
c      this program reads the coordinates of any point on the reflector
c      and determines the cooresponding coordinates on the near field
c      plane
      implicit real*8 (a-h)
      implicit real*8 (o-z)
      dimension x(9,9),y(9,9),z(9,9),k(81),l(81),xa(9,9),ya(9,9)
      real*8 l1x,l1y,l1z,l1,ul1x,ul1y,ul1z
      real*8 r,ul2x,ul2y,ul2z
      real*8 pdfdx,pdfdy,pdfdz,absnrm1
      real*8 nrmlx,nrmly,nrmlz

      open(12,file='data')
      open(13,file='res',status='old')
      write(6,*) 'enter distortion factor t'
      read(5,*) t
      xlambd = 0.1
      nperiod = 1
      f = 1.0
      ymax = 1.1
      ymin = 0.1
      d = 1.
      delref = 0.125
      zp = 1.
      del = t * xlambd
      xf = 0.0
      yf = 0.0
      zf = 1.0
      pi = 3.14159265
      omega = 2.0 * pi * nperiod/(ymax-ymin)
      c= 2 * pi/xlambd
      zaa = zp
      nrefgp = d/deref + 1
      do 10 i=1,nrefgp
      do 20 j=1,nrefgp
         read(13,3)k(i),l(j),x(i,j),xa(i,j),y(i,j),ya(i,j),z(i,j)
3        format(2i3,5f11.7)
         l1x = xf - x(i,j)
         l1y = yf - y(i,j)
         l1z = zf - z(i,j)
         l1 = sqrt(l1x**2 + l1y**2 + l1z**2)
         pdfdx = -x(i,j)/(2.0*f)
         pdfdy = -y(i,j)/(2.0*f) - del*omega*sin(omega*(ymax
1           -y(i,j)))
         pdfdz = 1.0
         absnrm1 = sqrt(pdfdx**2 + pdfdy**2 + pdfdz**2)
         nrmlx = pdfdx/absnrm1
         nrmly = pdfdy/absnrm1
         nrmlz = pdfdz/absnrm1
         ul1x = l1x / l1
         ul1y = l1y / l1
         ul1z = l1z / l1
         r = 2.0*(nrmlx*ul1x+nrmly*ul1y+nrmlz*ul1z)
         ul2x = ul1x - r*nrmlx
         ul2y = ul1y - r*nrmly
         ul2z = ul1z - r*nrmlz
c         in original z(i,j) was z
         xaa = (zaa-z(i,j))*(ul2x/ul2z) + x(i,j)
         yaa = (zaa-z(i,j))*(ul2y/ul2z) + y(i,j)
         write(12,5)k(i),l(j),x(i,j),xaa,y(i,j),yaa,z(i,j),zaa
5        format(2i3,6f10.5)
20       continue
10      continue
      close(13)
      close(12)
      end

```

gasdev.f

```
function gasdev()
c      returns a normally distributed deviate with zero mean
c      and unit variance
double precision rand
      data iset/0/
      data gset/0.0/
      if(iset.eq.0) then
1      v1 = 2. * rand() - 1.
      v2 = 2. * rand() - 1.
      r = v1**2 + v2**2
      if(r.ge.1)go to 1
      fac = sqrt(-2.*log(r)/r)
      gset = v1 * fac
      gasdev = v2 * fac
      iset = 1
      else
      gasdev = gset
      iset = 0
      endif
      return
      end
```

vary1k.f

```
program vary
  implicit double precision (a-h)
  implicit double precision (o-z)
  double precision xamp(8),yamp(8)
  common /partial/ pdfdx,pdfdy,pdfdz
  common /distort/ del,omega,xamp1,yamp1
  integer type
  common /phys/ f,xf,yf,zf,zp,xmin,xmax,ymin,ymax,freq,type
  real maxerr(20,20),avgerr(20,20),rmserr(20,20)
  integer error(20,20)
  integer npts(8),nerrors(8)
#define MAX_CURVES 8
#define MAX_POINTS 50
c      character*80 filename,plttl,xttl,yttl,zttl
#ifndef ERROR
  real xdata(50,8)
  real ydata(50,8)
  real avgitr
  common /perf/ avgitr
#else  ERROR
  real xdata(50,8)
  real adata(50,8)
  real rdata(50,8)
  real mdata(50,8)
  real sigma(50,8)
  real inacc(50,8)
#endif ERROR
  common /plot/ idist,igrid,
1 maxerr(20,20),avgerr(20,20),rmserr(20,20),error(20,20)
  data xamp /0.00, 0.01, 0.02, 0.03, 0.04, 0.05, 0.06, 0.07/
  B
  data yamp /0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00, 0.00/
  integer atime(3),iday,imonth,iyear
500  format(i2.2,'/',i2.2,'/',i2.2,' ', i2.2,':',i2.2.'i2.2)
  call itime(atime)
  call idate(iday,imonth,iyear)
  write(6,500)imonth,iday,iyear,atime
  B
  fmaxerr=.000001

  ymax=1.1
  ymin=0.1
  xmax=0.5
  xmin=-0.5
  type = 1

  infile1=1024
  idiv = ifix(log(float(infile1))/log(2.0)-2.5)
  ngrids = 2*ifix(log(float(infile1))/log(2.0)-2.5)
  infile1=infile1+1

  f = 1.0

  xf = 0.0
  yf = 0.0
  zf = 1.0

  zp = 1.0

  periods = 1.0
  omega = 2.0 * 3.14159265 * periods / (ymax-ymin)

  freq=30500000000.
c      Wave number
```

vary1k.f

```
k = 2.0 * 3.141592650 / (300000000/freq)

open(7,file="results.dat")
open(99,file="contour.dat")
min_dist=1
max_dist=7

997  read(5,997) i
      format(i3)
      if(i.lt.min_dist.or.i.gt.max_dist) then
          write(6,999)i
          format(" bad distortion selector:",i4);
          stop
      else
          write(6,998)i, xamp(i), yamp(i)
          format("doing iteration #",i2,"; ",g10.4,".",g10.4)
      endif

c      do 10 i=min_dist,max_dist
      idist=i
      xamp=xamp(i)
      yamp=yamp(i)
      write(7,105)
      105 format('avgerr.wpg')
      write(7,106) xamp,yamp
      106 format(' rnfpg error analysis'
      1 ' amplitude of (x,y) distortion = (' 
      2 ,d18.10,',',d18.10,')')

      xlambd = 0.1
      t = xamp
      del = t * xlambd

      open(4,file="ph1.dat",FORM='unformatted')
      call rnfpg(infile1,fmaxerr)
      close(4)
      open(3,file="ph1.dat",FORM='unformatted')
      open(4,file="ph1f.dat",FORM='unformatted')
      call fixphi(infile2)
      close(4)
      close(3)
      21  npts(i) = j-1
      10  continue
          call itime(atime)
          call idate(iday,imonth,iyear)
          write(6,500)imonth,iday,iyear,atime
      stop
      end
```